

Double- and Triple-RF systems for MAX4^U

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Outline

1. MAX4^U and MAX IV RF system
2. Double-RF
3. Triple-RF

Toolbox used

[Pycolleff \(GitHub\)](#)

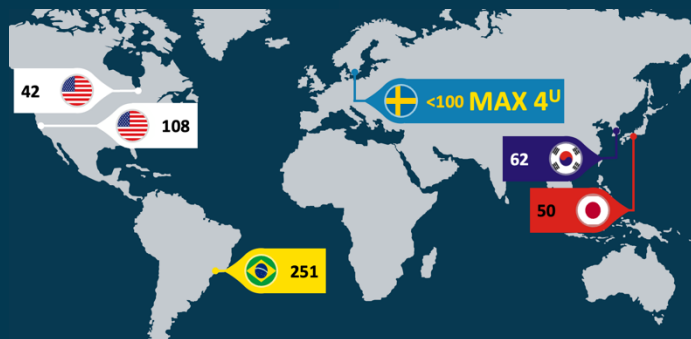
[ALBuMS, Mbtrack2 \(GitLab\)](#)

Mbtrack (tracking)

MAXIV

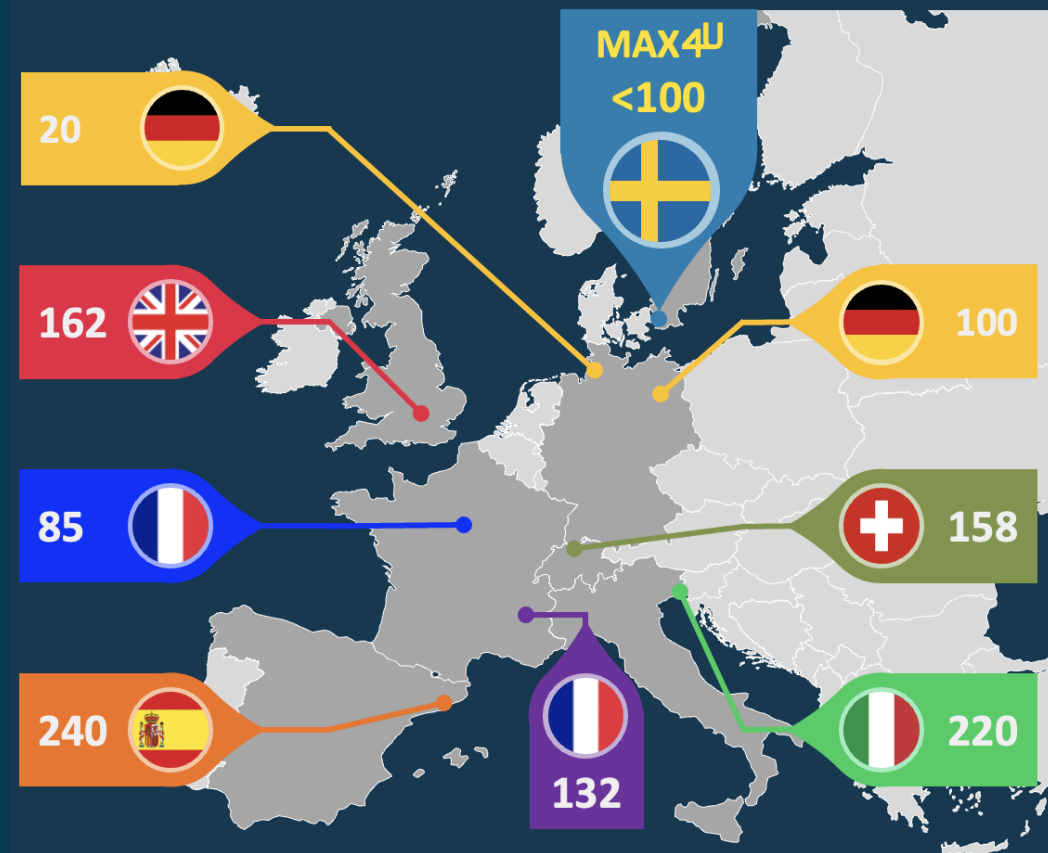


Securing leadership, excellence, resilience, and relevance of Swedish research with X-rays for the next decades



A "surgical" upgrade of our 3GeV ring from 328 to below 100pm·rad

Horizontal Emittance [pm·rad]



Relevant parameters for MAX4^U lattice candidates (CDR)

R3: MAX IV 3GeV Ring

AR: Absolute Requirement

SG: Stretched Goal

	R3 (as designed)	AR (i01-04-01-01)	SG (n01-01-01-01)	Units
Natural emittance	328	95	65	pm rad
Natural energy spread	7.69	7.55	8.46	10 ⁻⁴
RF voltage	1.8	1.0	1.0	MV
Momentum compaction factor	3.06	0.944	0.540	10 ⁻⁴
Energy loss per turn	364	414	474	keV
Natural bunch length	29	22	19	ps
Damping times (H/ V/ L)	15.73 / 29.05 / 25.19	14.75 / 25.51 / 20.08	11.44 / 22.29 / 21.18	ms

Design current: 500 mA uniform filling

Requirements for bunch lengthening

R3 delivery conditions

- Beam current: 400 mA
- RF voltage: 1.13 MV
- Natural bunch length: 38 ps
- Double-RF system (2 passive HC3s): **180 ps (x 4.7 lengthening)**
- Beam lifetime with HC3s: 15 h
- Essential for HOMs rejection, alleviating IBS

MAX4^U lattices

- Beam current: 500 mA
- RF voltage: 1.00 MV
- Natural bunch length: ~ 20 ps
- Ideal double-RF performance: **~120 ps (x 6 lengthening)**
- Higher lengthening factors required → Triple-RF system

The MAX IV RF system

Double-RF system

Triple-RF system 

Main Cavity



HC3 (Passive)



HC5 (Active)



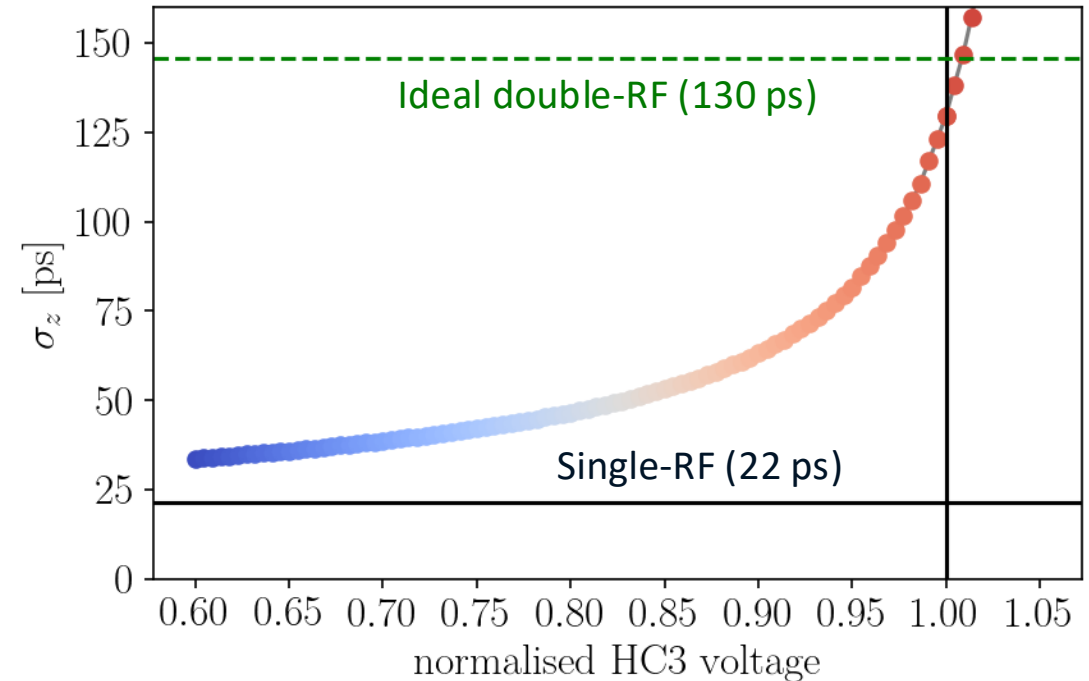
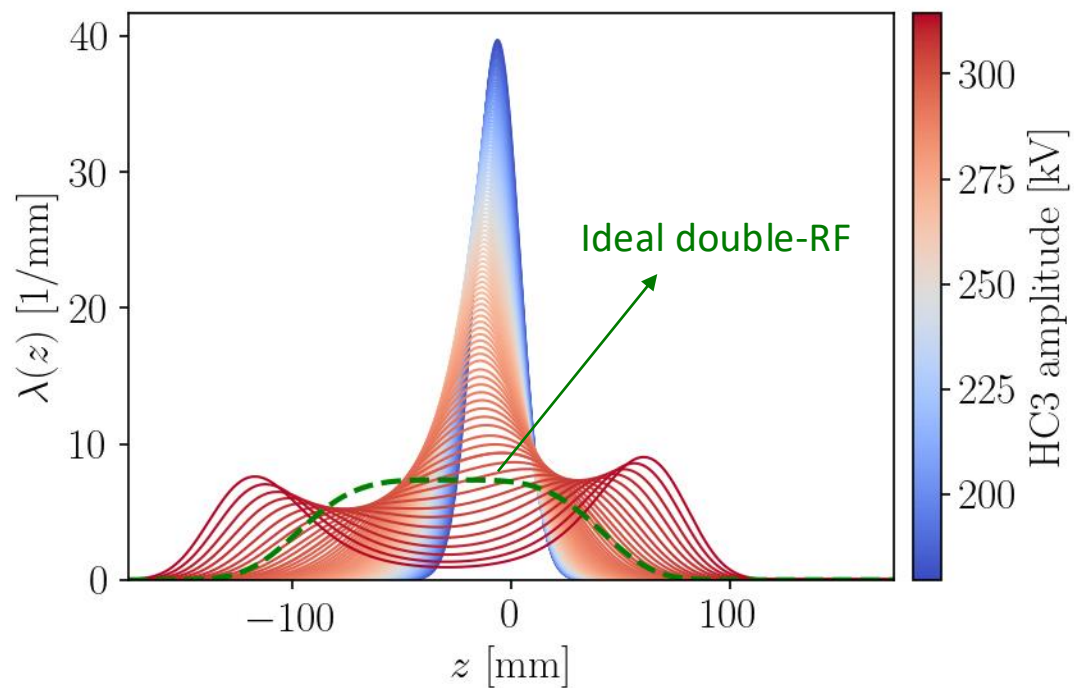
Images by Åke Andersson



Double-RF

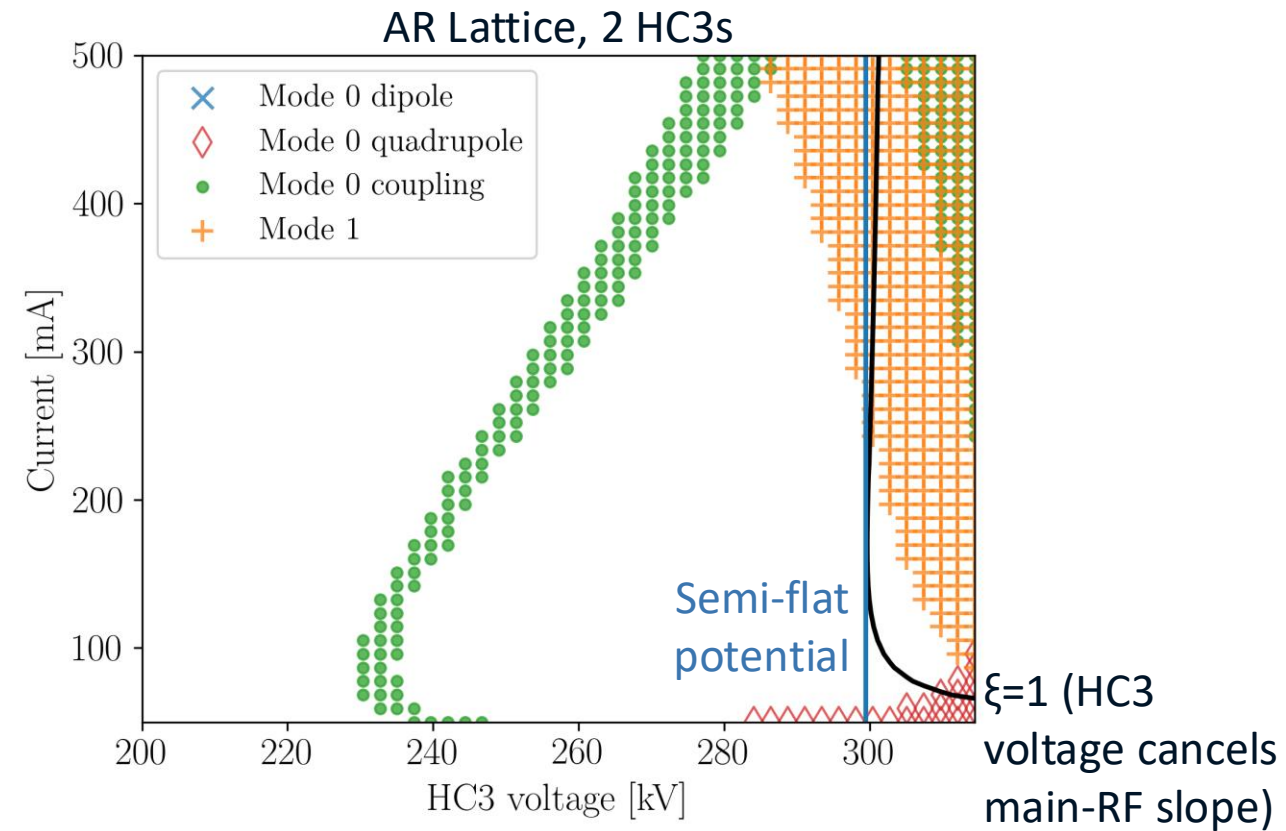
Double-RF with passive HC3

- With $V_{\text{RF}} = 1.0$ MV, $U_0 = 450$ keV, ideal HC3 amp around 300 kV
- Example for AR lattice. Factor 6 of lengthening



Longitudinal multibunch beam stability

- Stability estimates using Gaussian LMCI model¹
- Bosch grids²: where in parameter-space the beam is predicted to be unstable and why
- Passive HC3 cavities
- Semi-flat potential = correct amplitude but not phase

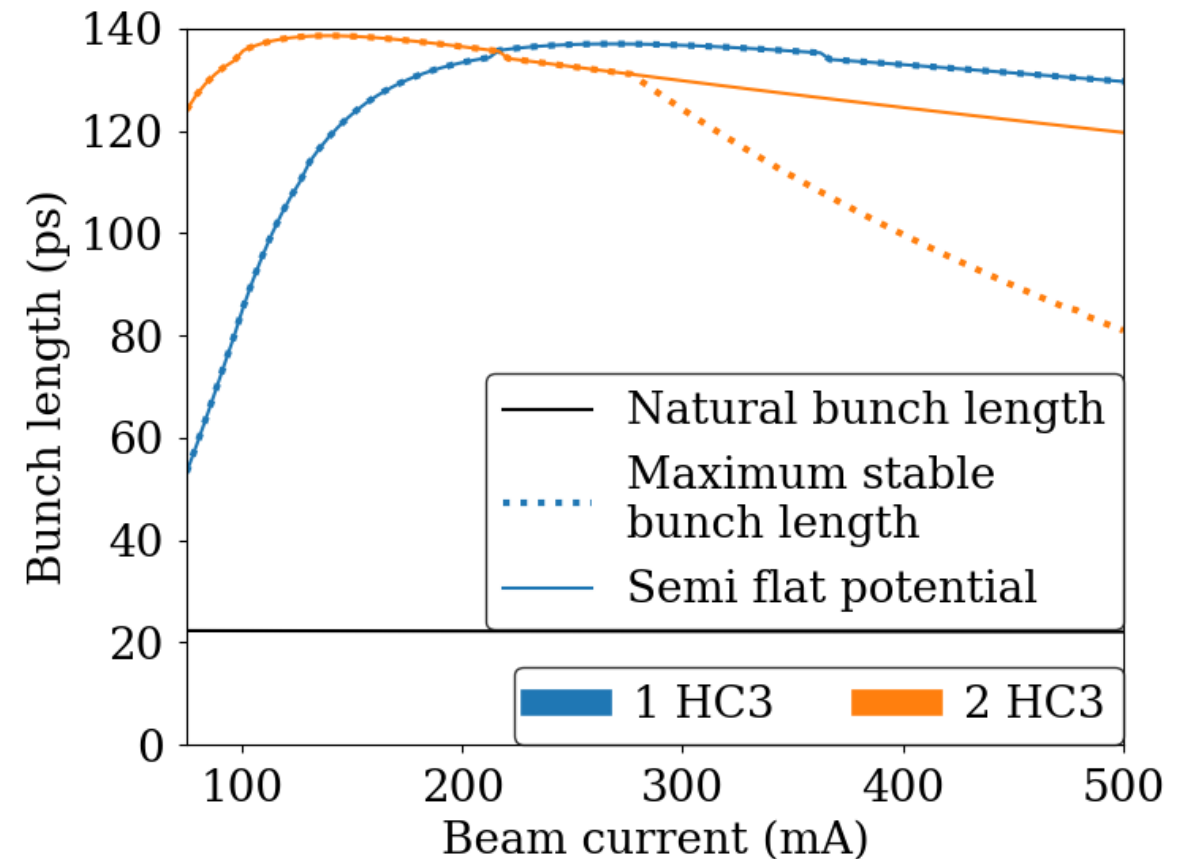


¹ M. B. Alves, “Theoretical models for longitudinal coupled-bunch instabilities driven by harmonic cavities in electron storage rings”, Phys. Rev. Accel. Beams **28** 03440 (2025)

² A. Gamelin, V. Gubaidulin, M. B. Alves, T. Olsson, “Semianalytical algorithms to study longitudinal beam instabilities in double rf systems” Phys. Rev. Accel. Beams **28** 054401 (2025)

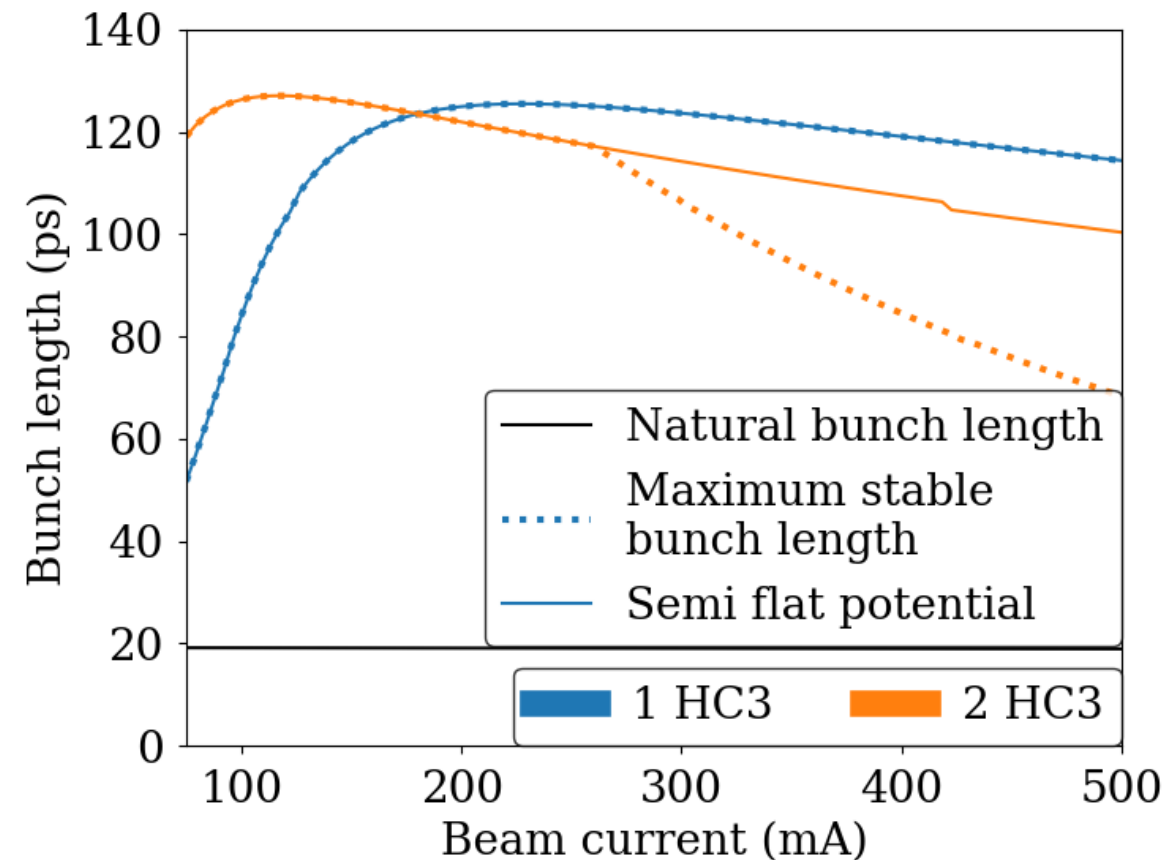
Mode 1: maximum stable bunch lengths – AR Lattice

- Assuming Mode 0 is controlled by mode-0 damper (TBC)
- Flat potential is where HC3 field level is same as for ideal lengthening
- Single HC3 cavity allows semi-flat potential to be reached at 500 mA



Mode 1: maximum stable bunch lengths – SG Lattice

- Assuming Mode 0 is controlled by mode-0 damper (TBC)
- Flat potential is where HC3 field level is same as for ideal lengthening
- Single HC3 cavity allows semi-flat potential to be reached at 500 mA



Analytical formula for Mode 1 (PTBL) threshold*

Valid for passive double-RF

"Correction" factor

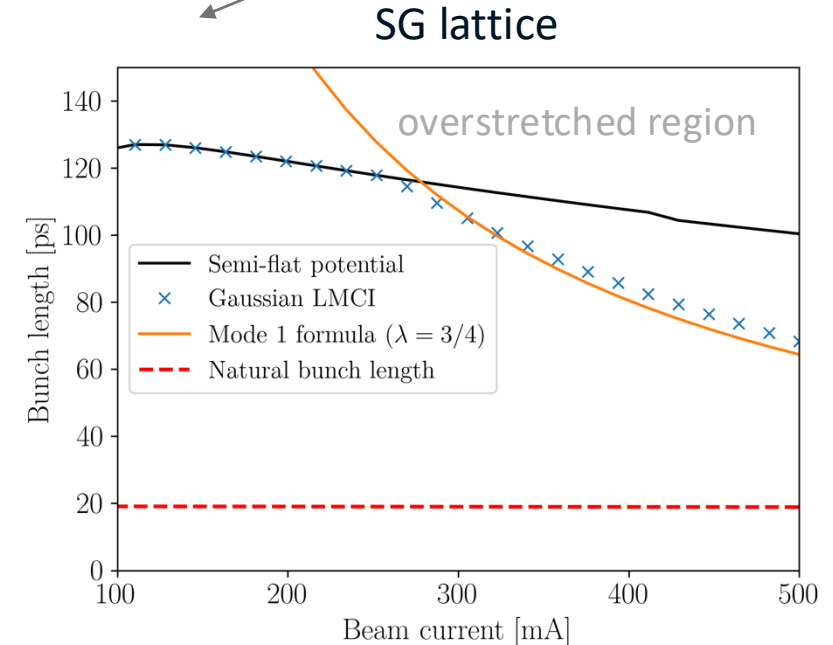
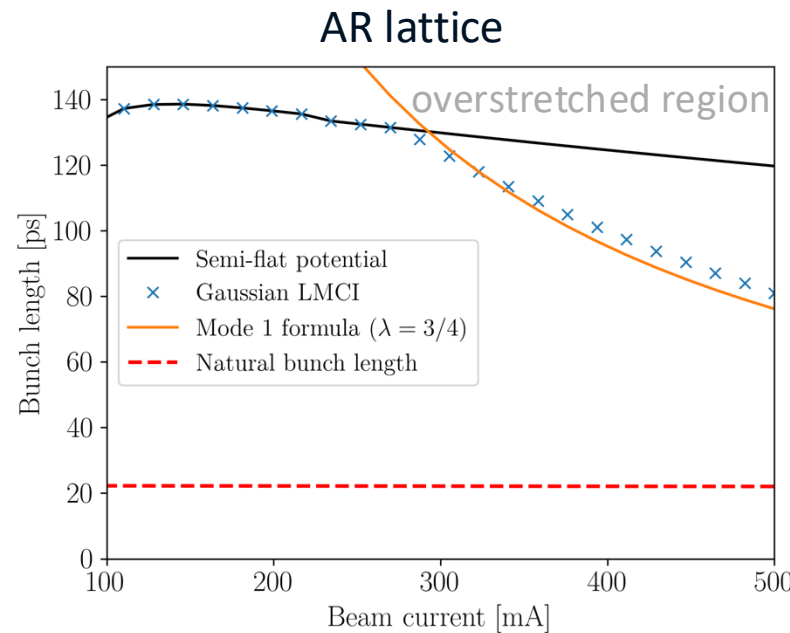
$$\sigma_\tau = \lambda \frac{T_0 \sigma_\delta}{I_0 (R/Q) n^2} \sqrt{\frac{E_0 \alpha \hat{V}_{\text{rf}}}{2\pi e F_n h^3}}$$

2 HC3s
n = 3
F_n = 1

$$\omega_s \sigma_\tau = \lambda \alpha \sigma_\delta$$

$\lambda = 1$ Linear dynamics
Gaussian bunch

$\lambda = 3/4$ Good match with
Gaussian LMCI

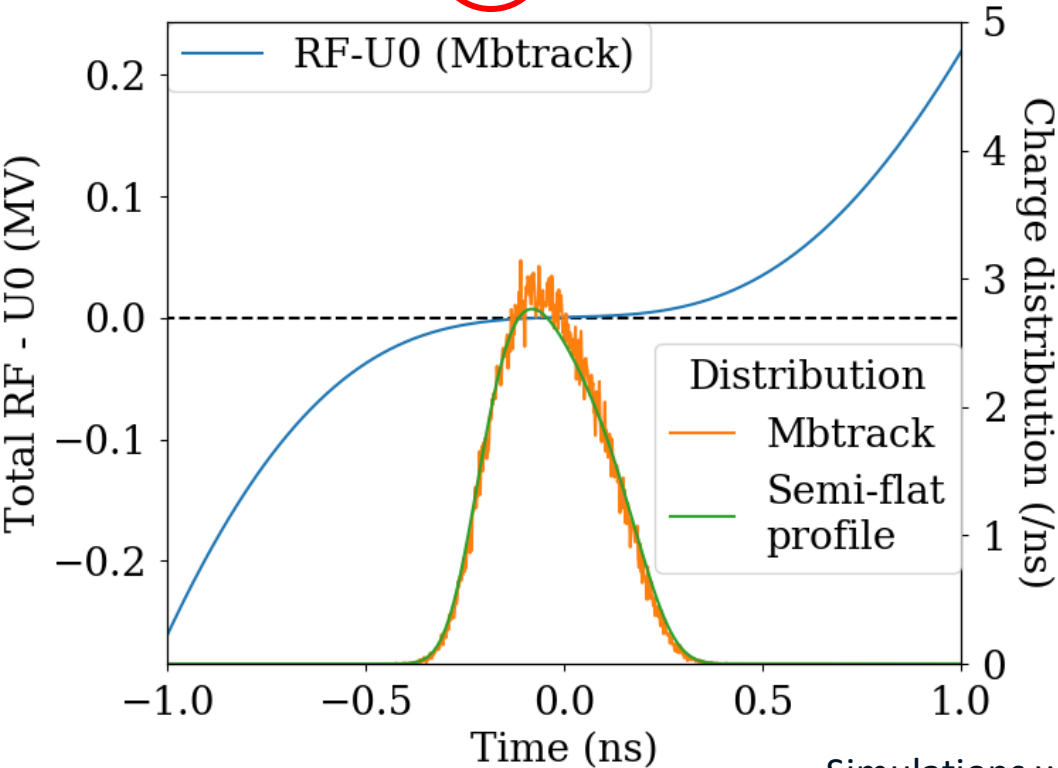


*Derivation in Appendix B of M. B. Alves, Phys. Rev. Accel. Beams **28** 03440 (2025)

Stable bunch profiles with single HC3

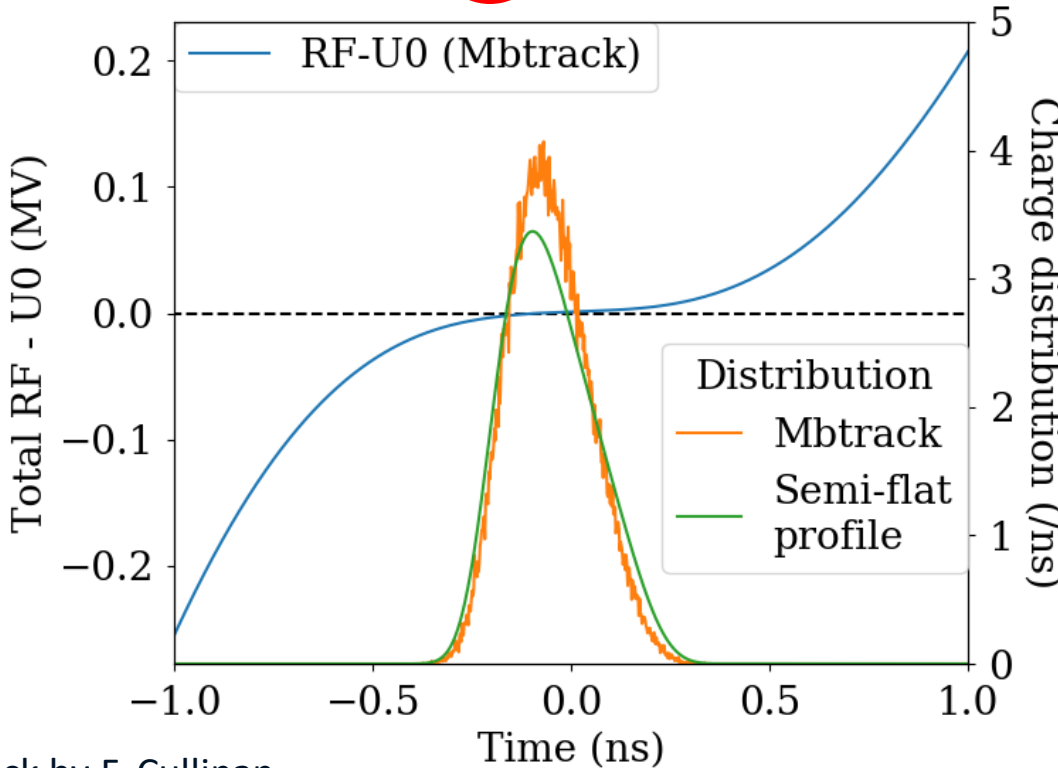
AR Lattice (natural bunch length=22 ps)

	Semi-flat	Mbtrack max. stable
Bunch length (ps)	130	126
HC3 voltage (kV)	299.5	298.4



SG Lattice (natural bunch length=19 ps)

	Semi-flat	Mbtrack max. stable
Bunch length (ps)	114	101
HC3 voltage (kV)	288.1	285.5



Simulations with Mbtrack by F. Cullinan



Triple-RF (work in progress)

Triple-RF with 2 passive HC3s + 1 active HC5

- Given V_{RF} , U_0 and harmonics $\rightarrow$ amplitudes and phases that cancel derivative of total voltage up to Nth order*
- Triple-RF: 4th order, Super-Flat Potential (SFP)

$$V_{RF} = 1.0 \text{ MV}$$

$$U_0 = 450 \text{ keV}$$

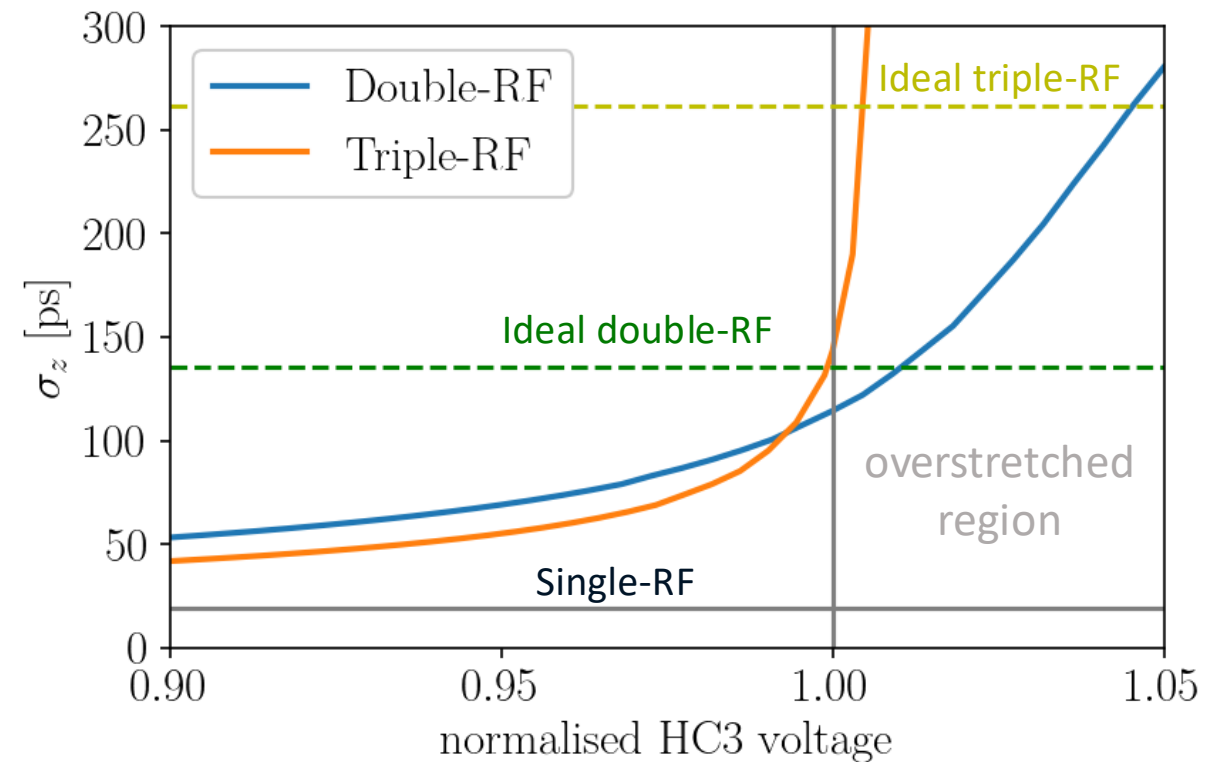
	Main Cavities		3rd harmonic (HC3)		5th harmonic (HC5)	
	Amp [kV]	Phase [deg]	Amp [kV]	Phase [deg]	Amp [kV]	Phase [deg]
Double-RF	1000	149.6	293	-11.1	--	--
Triple-RF	1000	148.2	434	-11.7	86	172.9

- Higher HC3 fields required in a triple-RF
- HC5 must be active

*F. Cullinan, P. Tavares, Å. Andersson, L. Malmgren,
 “Harmonic Cavity Parameters for Flat Potential to Arbitrary Order” MAX IV Internal Note 20240410

Bunch lengthening sensitivity

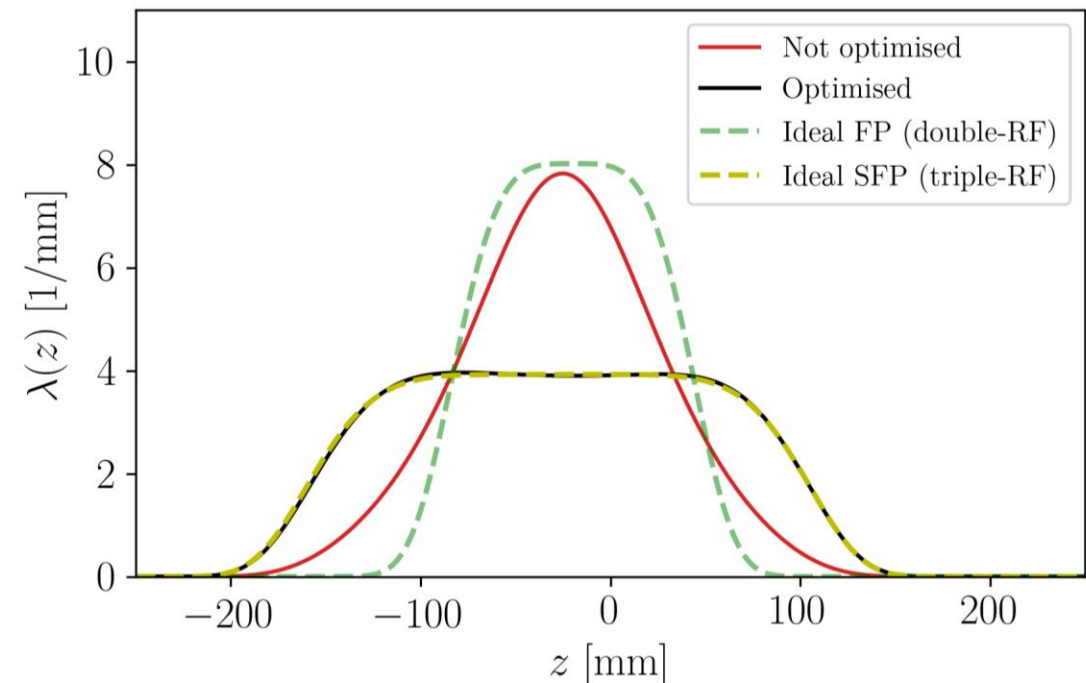
- Main and HC5 (active cavities) set to ideal amplitudes and phases
- Passive HC3 amp adjusted by detuning
- Bunch profiles much more sensitive to HC3 amp/phase variations
- Possible solutions to compensate for this limited control:
 - MC and HC5 adjustments
 - Active HC3s



Impact of finite Q factor of cavities - AR Lattice

	RF Voltage [MV]	HC3 Amp [kV]	HC5 Amp [kV]	σ_z ideal FP [ps]	σ_z ideal SFP [ps]	σ_z actual [ps]
Not Optimised	1.00	444.6	88.0	146	275	187 (-32%)
Optimised	1.33	626.5	123.1	133	259	258

- Main and HC5 amps used as optimisation knobs
- Benchmarking with Mbtrack in progress
- High HC3 voltage becomes challenging again

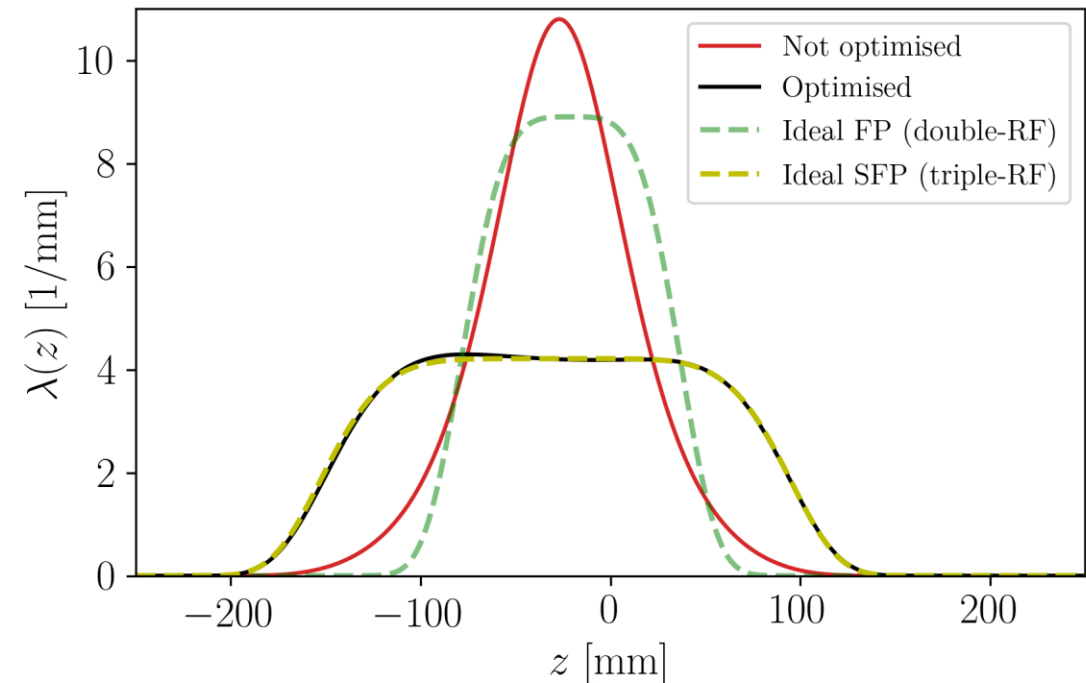


Also studied in He *et al.*, *NIM A* **1080**, 170672 (2025) “Impact of short-range wakefields from radio-frequency cavity resonant modes on bunch lengthening”

Impact of finite Q factor of cavities - SG Lattice

	RF Voltage [MV]	HC3 Amp [kV]	HC5 Amp [kV]	σ_z ideal FP [ps]	σ_z ideal SFP [ps]	σ_z actual [ps]
Not Optimised	1.00	425.9	83.9	135	262	143 (-45%)
Optimised	1.46	679.2	135.0	120	241	240

- Main and HC5 amps used as optimisation knobs
- Benchmarking with Mbtrack in progress
- High HC3 voltage becomes challenging again



Also studied in He *et al.*, *NIM A* **1080**, 170672 (2025) “Impact of short-range wakefields from radio-frequency cavity resonant modes on bunch lengthening”

Summary and next steps

- Low- α feature of MAX4^U brings challenges to bunch lengthening and stability
- **Double-RF**
 - Bunch lengthening: MAX4^U $\sigma_z = 120\text{ps}$ (factor 6) vs. MAX IV R3 $\sigma_z = 180\text{ps}$ (factor 5)
 - Mode-0 expected to be controlled with damper
 - Mode-1 stable only with single passive HC3
- **Triple-RF (work in progress)**
 - Much more sensitive to cavity parameters variations than double-RF
 - “Short-range wakes” from fundamental modes are relevant and can be compensated
- **Next steps**
 - Evaluation of collective beam instabilities with triple-RF system
 - Include full impedance model: Geometric, RW, HOMs, IDs
 - Experimental tests
 - Double-RF with 1 HC3
 - Triple-RF system



MAX4^U page



<https://www.maxiv.lu.se/beamlines-accelerators/max-4u/>

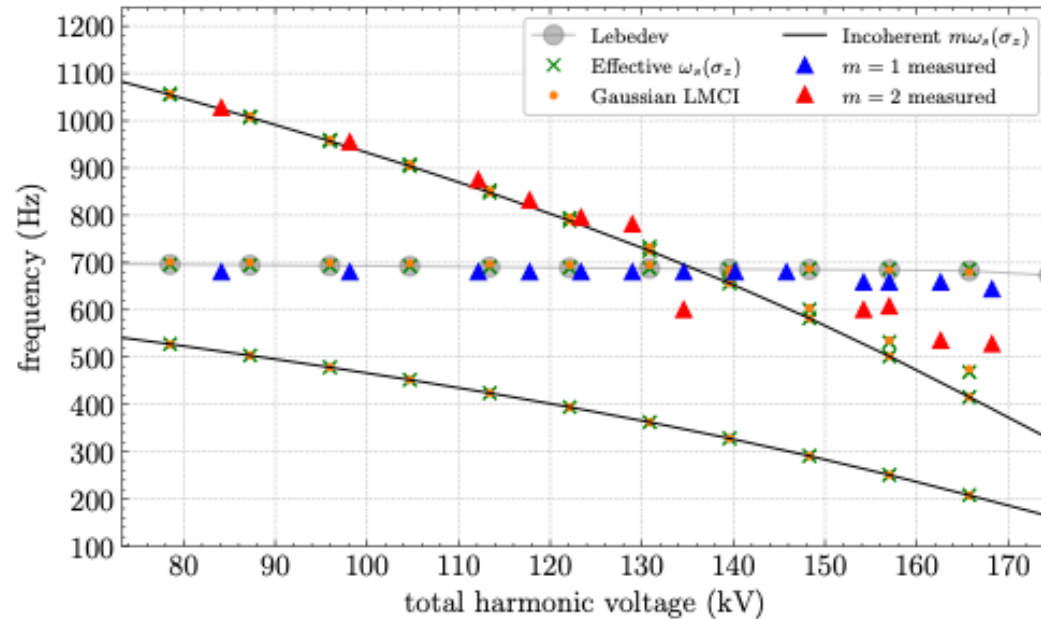


Backup Slides

HC3-related instabilities at MAX IV

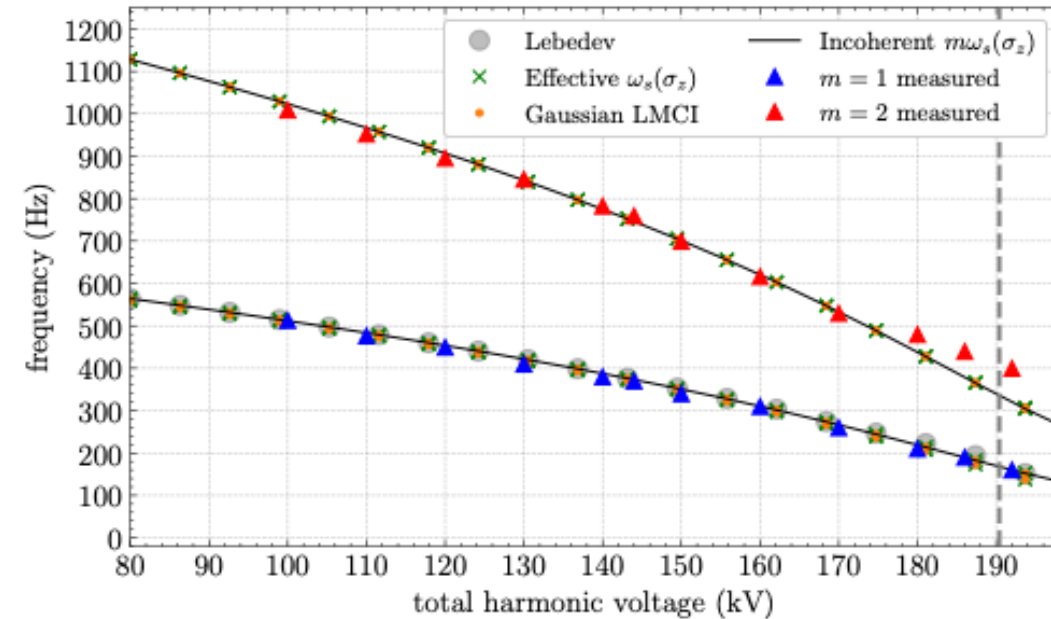
Measurements below threshold

Mode 0 Coupling



$V_{RF} = 650$ kV, $I_0 = 50$ mA

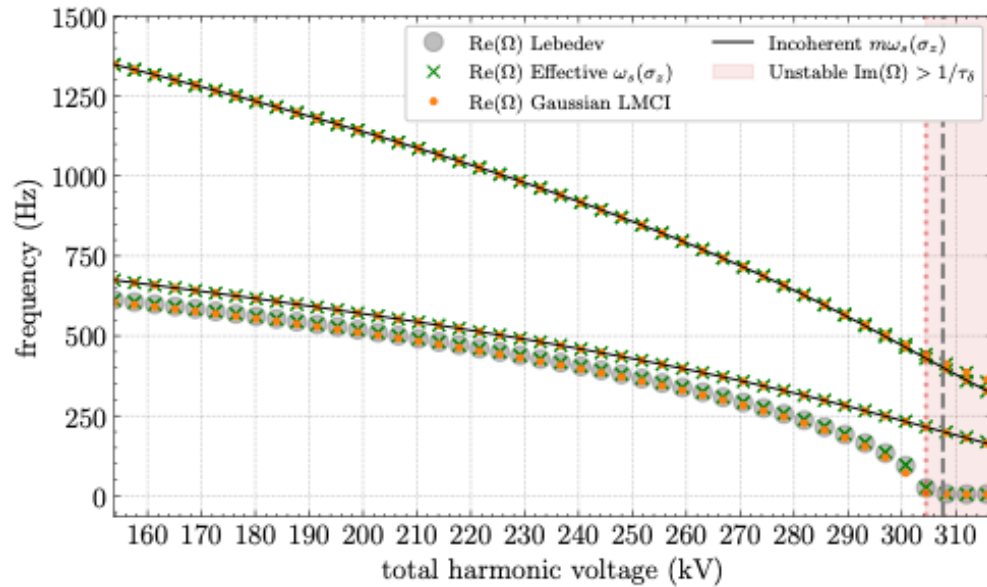
Mode 1



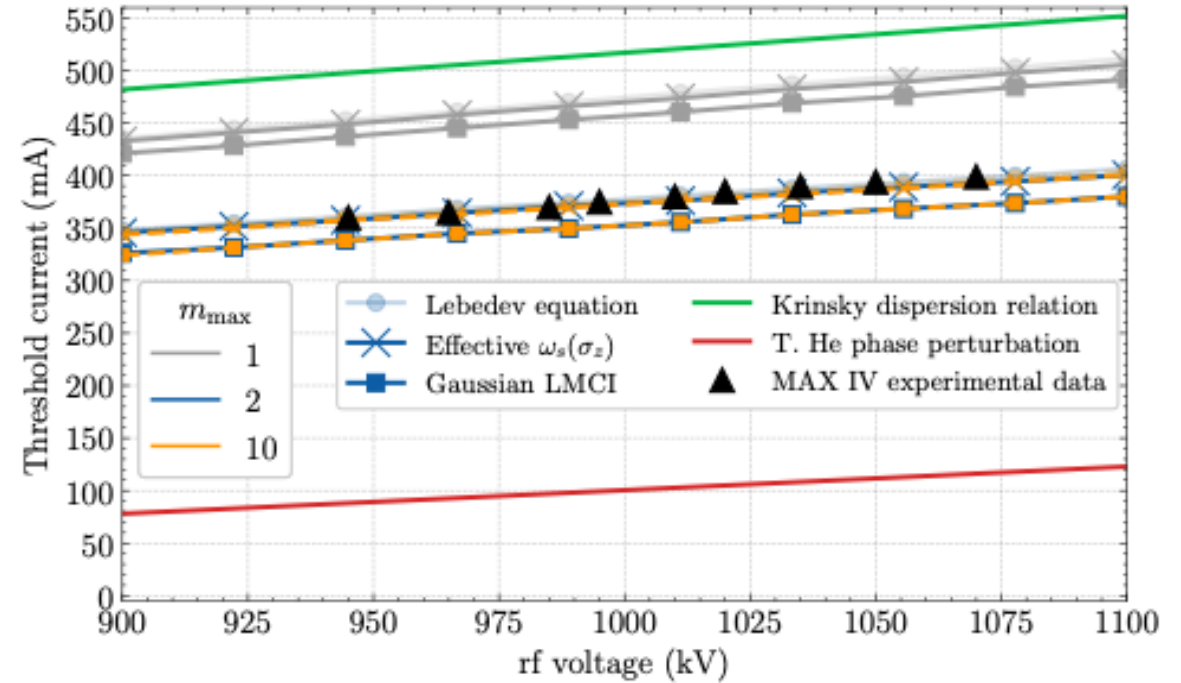
$V_{RF} = 689$ kV, $I_0 = 90$ mA

M. B. Alves, “Theoretical models for longitudinal coupled-bunch instabilities driven by harmonic cavities in electron storage rings”, Phys. Rev. Accel. Beams **28** 03440 (2025)

Mode 1 thresholds at MAX IV



$V_{RF} = 1.0$ MV, $I_0 = 300$ mA, 3 HC3s



2 HC3s, $V_{RF} = 1.0$ MV: 400mA is achieved

M. B. Alves, “Theoretical models for longitudinal coupled-bunch instabilities driven by harmonic cavities in electron storage rings”, Phys. Rev. Accel. Beams **28** 03440 (2025)